

Flow Matching for Generative Modeling

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Context: Generative Modeling

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Since sampling p_0 is easy, the only difficulty is learning f .

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Yaron Lipman, Ricky T. Q. Chen, Heli Ben-Hamu, Maximilian Nickel, Matt Le

Instead of learning f directly, define a **continuous flow**:

$$\frac{dx_t}{dt} = v_t^*(x_t),$$

such that: $x_1 = x_0 + \int_0^1 v_t^*(x_t) dt$, where $x_0 \sim p_0$, $x_1 \sim p_{\text{data}}$.

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$$x_1 = x_0 + \int_0^1 v_t^*(x_t) dt \approx x_0 + \int_0^1 v_t^\theta(x_t) dt$$

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Model Prediction / Loss: The network predicts a velocity field $v_t^\theta(x_t)$ along the chosen path, trained with:

$$\mathcal{L}(\theta) = \mathbb{E}_{x_0, x_1, t} \left[\|v_t^\theta(x_t) - \dot{x}_t\|^2 \right]$$

where $\dot{x}_t$ is the derivative of the chosen path at time t .

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Examples of Probability Paths:

- ▶ **Straight / linear paths:** $x_t = (1 - t)x_0 + tx_1$ — simplest deterministic interpolation

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- ▶ **Diffusion-style Variance-Exploding path:** Conditional vector field:

$$w_t(x \mid x_0) = -\frac{\sigma'_{1-t}}{\sigma_{1-t}}(x - x_0)$$

where σ_t is the noise schedule. Equivalent to VP or VE schedule in diffusion models.

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- ▶ **Dirichlet flows (on simplex):** Conditional paths:
 $p_t(x \mid x_1 = e_i) = \text{Dir}(x; \alpha = 1 + t \cdot e_i)$, initial
 $p_0 = \text{Dir}(x; \alpha = (1, \dots, 1)^T)$

Ref: *Dirichlet Flow Matching with Applications to DNA Sequence Design*, Hannes Stark et al.

Flow Matching vs. DDIM

DDIM:

- To generate a sample from noise to data:

$$x_1 = x_0 + \int_0^1 v_t dt, \quad v_t = \frac{f^\theta(x_t, t) - x_t}{1 - t}$$

Flow Matching vs. DDIM

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- ▶ Learned by minimizing the conditional prediction loss along the path:

$$\mathcal{L}_{\text{DDIM}} = \mathbb{E}_{x_0, x_1, t} \left[\|f^\theta(x_t, t) - x_1\|^2 \right]$$

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FM:

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$$x_1 = x_0 + \int_0^1 v_t^\theta dt$$

- ▶ Learned by minimizing the conditional prediction loss along the path:

$$\mathcal{L}_{\text{FM}} = \mathbb{E}_{x_0, x_1, t} \left[\|v^\theta(x_t, t) - (x_1 - x_0)\|^2 \right]$$

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Equivalent Formulations and Concurrent Work:

- ▶ **Stochastic Interpolants: A Unifying Framework for Flows and Diffusions**

Michael S. Albergo, Nicholas M. Boffi, Eric Vanden-Eijnden

- ▶ **Flow Straight and Fast: Learning to Generate and Transfer Data with Rectified Flow**

Xingchao Liu, Chengyue Gong, Qiang Liu

Multisample Flow Matching: Straightening Flows with Minibatch Couplings

Aram-Alexandre Pooladian, Heli Ben-Hamu, Carles Domingo-Enrich, Brandon Amos, Yaron Lipman, Ricky T. Q. Chen

- ▶ Standard Flow Matching samples $x_0 \sim p_0$ and $x_1 \sim p_1$ **independently**.

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- ▶ **Idea:** Correlate x_0 and x_1 across the minibatch to produce straighter paths and more efficient learning.

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Multisample Flow Matching Algorithm:

1. Sample minibatches: $\{x_0^{(i)}\}_{i=1}^k \sim q_0(x_0)$, $\{x_1^{(i)}\}_{i=1}^k \sim q_1(x_1)$

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3. Define the joint discrete distribution:

$$q_k(x_0, x_1) = \frac{1}{k} \sum_{i,j=1}^k \delta(x_0 - x_0^{(i)}) \delta(x_1 - x_1^{(j)}) \pi(i, j)$$

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4. Train the velocity field along interpolated paths sampled from $q_k(x_0, x_1)$

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How to choose the minibatch coupling π :

- ▶ **Batch Optimal Transport (BatchOT):** Compute the exact OT plan between minibatch samples to produce a *permutation-like* doubly-stochastic matrix. Leads to nearly straight interpolated paths. Complexity: $O(k^3)$ for a batch of size k (Hungarian or network simplex algorithms).

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More prosaically, reassign (in a hard or soft manner) the starting noises to the endpoints, to minimize the total target displacement.

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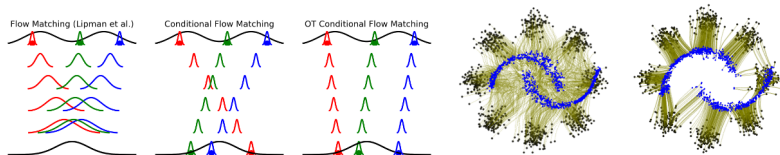
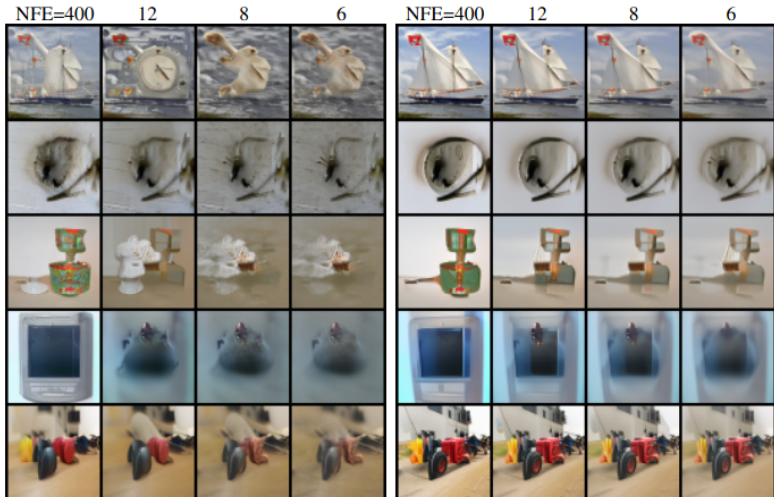


Figure: Reassigning prior samples "uncrosses" the target trajectories.

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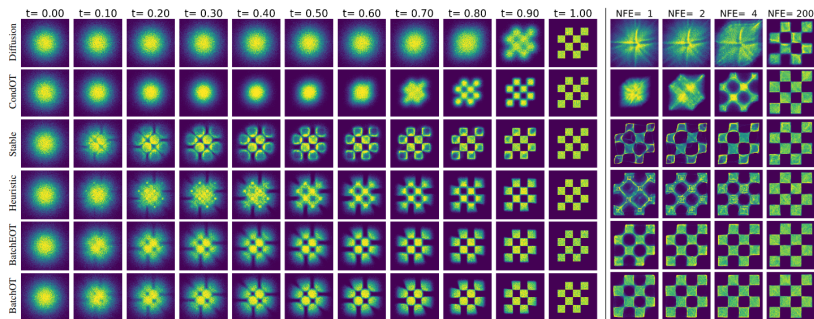


Flow Matching

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Equivalent formulation and Concurrent Work:

- ▶ **Improving and Generalizing Flow-Based Generative Models with Minibatch Optimal Transport**

Alexander Tong, Kilian Fatras, Nikolay Malkin, Guillaume Huguet, Yanlei Zhang, Jarrid Rector-Brooks, Guy Wolf, Yoshua Bengio

On the Closed-Form of Flow Matching: Generalization Does Not Arise from Target Stochasticity

Quentin Bertrand, Anne Gagneux, Mathurin Massias, Rémi Emonet

- Recall the Flow Matching loss:

$$\mathcal{L}(\theta) = \mathbb{E}_{x_0 \sim p_0, x_1 \sim p_{\text{data}}, t \sim U([0,1])} \left[\|u_\theta(x_t, t) - \dot{x}_t\|^2 \right],$$

where $x_t = (1 - t)x_0 + tx_1$

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- The optimal velocity field for this loss has a closed-form solution. No stochasticity in the target is needed.

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Closed-form:

$$\text{If } x_t = (1 - t)x_0 + tx_1, \quad b(1) := x_1$$

$$\text{then } \hat{u}_M^*(x, t) = \sum_{j=1}^M \lambda(x, t) \frac{b(j) - x}{1 - t},$$

$$\text{where } \lambda(x, t) = \text{softmax} \left[- \frac{\|x - t b(l)\|^2}{2(1 - t)^2} \right]_{l=1, \dots, M}$$

- $b(j)$: samples from the dataset

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- ▶ Becomes a “classical” ML compression problem.

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- ▶ Becomes a “classical” ML compression problem.
- ▶ If too costly, can be approximated by Monte-Carlo.

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LEFM Training Objective:

$$\mathcal{L}_{\text{LEFM}}(\theta) = \mathbb{E}_{\substack{x_0 \sim p_0 \\ x_1 \sim \hat{p}_{\text{data}} \\ t \sim U([0,1]) \\ b(2), \dots, b(M) \sim \hat{p}_{\text{data}}}} \left[\|u_\theta(x_t, t) - \hat{u}_M^*(x_t, t)\|^2 \right]$$

with

$$x_t = (1 - t)x_0 + tx_1, \quad b(1) := x_1,$$

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► Almost deterministic target

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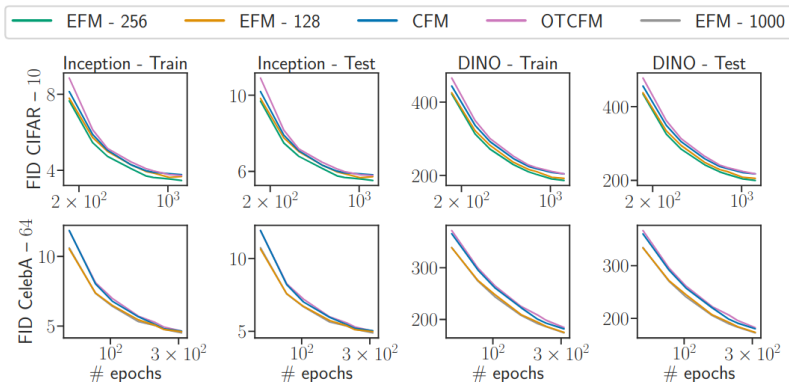


Figure 4: FID computed on the training set (50k) and the test set (10k) using multiple embeddings, Inception and DINOv2. Regressing against a more deterministic target (EFM - 128, 256, 1000) does not yield performance decreases. On the contrary, the more deterministic the target, the better the performance.

FlowAR: Scale-wise Autoregressive Image Generation Meets Flow Matching

Sucheng Ren, Qihang Yu, Ju He, Xiaohui Shen, Alan Yuille, Liang-Chieh Chen

Coarse-to-Fine Generation:

- ▶ Instead of generating the whole image at once, start with a very coarse version

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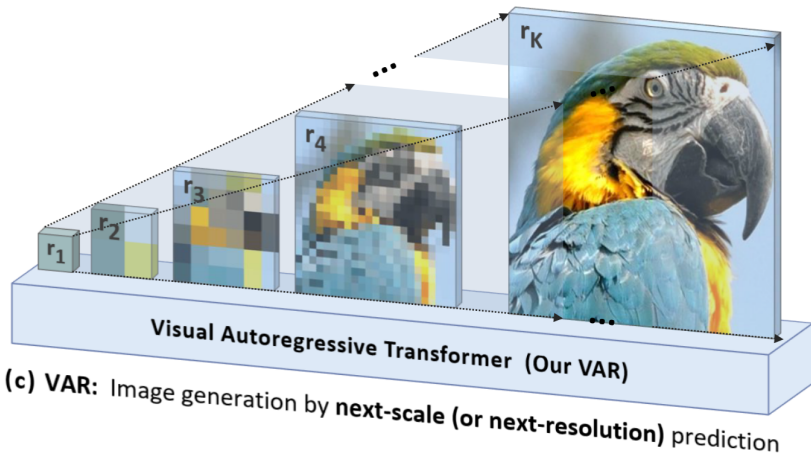
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Coarse-to-Fine Generation:

- ▶ Instead of generating the whole image at once, start with a very coarse version
- ▶ Generate a higher-resolution image conditioned on the upsampled coarse version
- ▶ Repeat the process to progressively refine the image

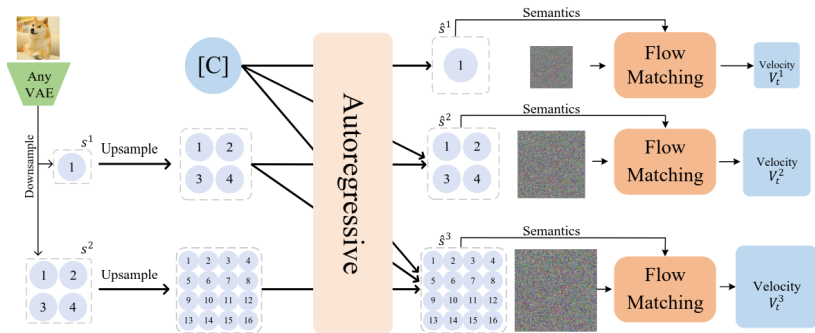
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method	type	params	FID ↓	IS ↑	Pre.↑	Rec.↑
BigGAN [6]	GAN	112M	6.95	224.5	0.89	0.38
GigaGAN [20]	GAN	569M	3.45	225.5	0.84	0.61
StyleGAN [40]	GAN	166M	2.30	265.1	0.78	0.53
ADM [12]	diffusion	554M	10.94	101.0	0.69	0.63
LDM [37]	diffusion	400M	3.60	247.7	-	-
U-ViT[5]	diffusion	287M	3.40	219.9	0.83	0.52
DiT [31]	diffusion	675M	2.27	278.2	0.83	0.57
SiT [2]	flow matching	675M	2.06	270.3	0.82	0.59
VQVAE-2 [36]	token-wise autoregressive	13.5B	31.11	45.0	0.36	0.57
VQGAN [14]	token-wise autoregressive	1.4B	15.78	74.3	-	-
RQTransformer [23]	token-wise autoregressive	3.8B	7.55	134.0	-	-
LlamaGen-B [42]	token-wise autoregressive	111M	5.46	193.6	0.83	0.45
ViT-VQGAN [51]	token-wise autoregressive	1.7B	4.17	175.1	-	-
LlamaGen-L [42]	token-wise autoregressive	343M	3.07	256.1	0.83	0.52
LlamaGen-XL [42]	token-wise autoregressive	775M	2.62	244.1	0.80	0.57
LlamaGen-3B [42]	token-wise autoregressive	3.1B	2.18	263.3	0.81	0.58
VAR-d12 [44]	scale-wise autoregressive	132M	5.81	201.3	0.81	0.45
FlowAR-S	scale-wise autoregressive	170M	3.61	234.1	0.83	0.50
VAR-d16 [44]	scale-wise autoregressive	310M	3.55	280.4	0.84	0.51
FlowAR-B	scale-wise autoregressive	300M	2.90	272.5	0.84	0.54
VAR-d20 [44]	scale-wise autoregressive	600M	2.95	302.6	0.83	0.56
FlowAR-L	scale-wise autoregressive	589M	1.90	281.4	0.83	0.57
VAR-d30 [44]	scale-wise autoregressive	2.0B	1.97	323.1	0.82	0.59
FlowAR-H	scale-wise autoregressive	1.9B	1.65	296.5	0.83	0.60

Conclusion

Thanks for your attention.